Your Softmax

Needs CPR 🐲

in Sequential Recommendation.

Achieving around 20% Improvement by just

Switching Your Output Softmax Layer!

To Copy, or not to Copy; That is a Critical Issue of the Output Softmax Layer in Neural Sequential Recommenders

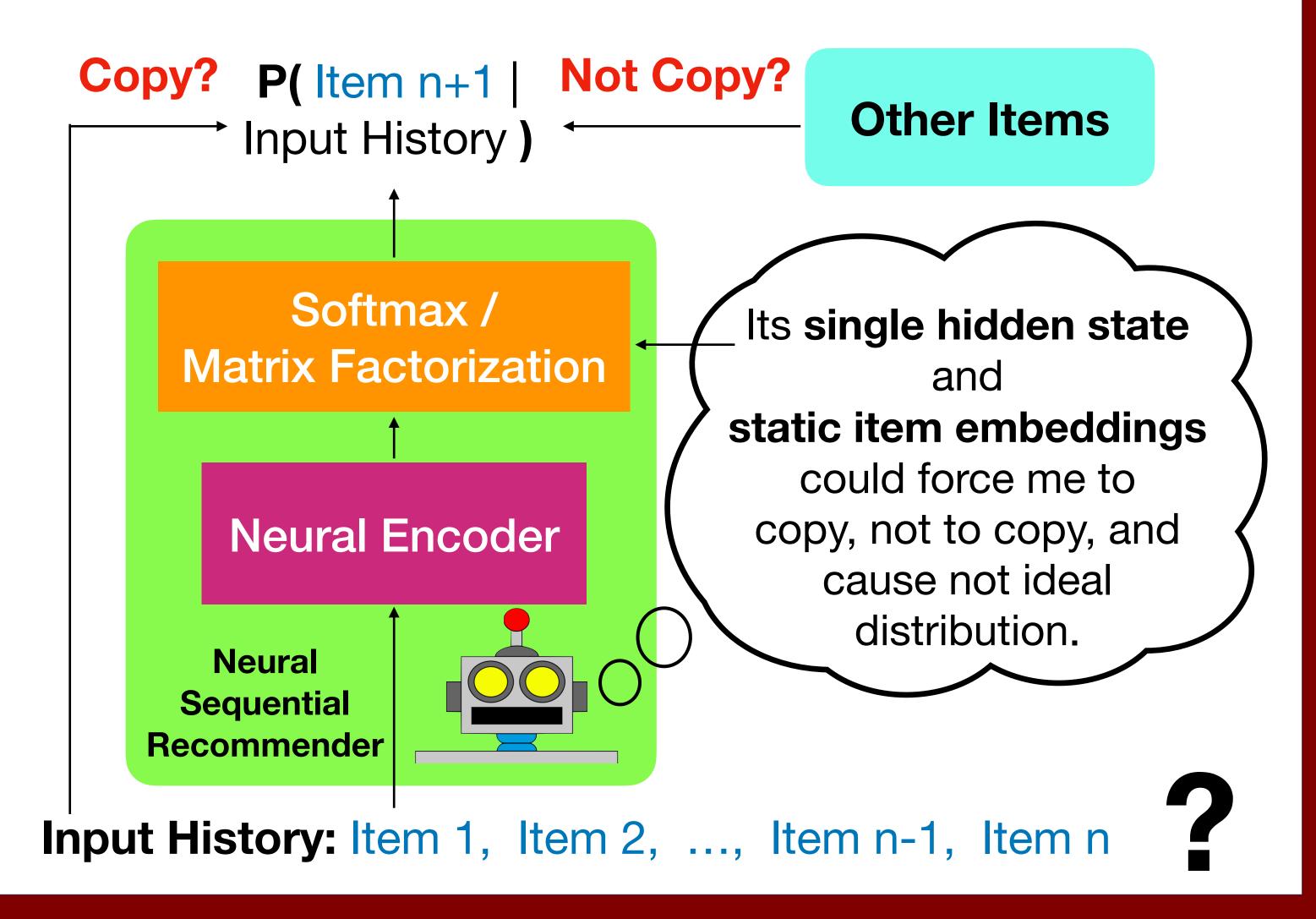
) amazon alexa

Haw-Shiuan Chang, Nikhil Agarwal, and Andrew McCallum

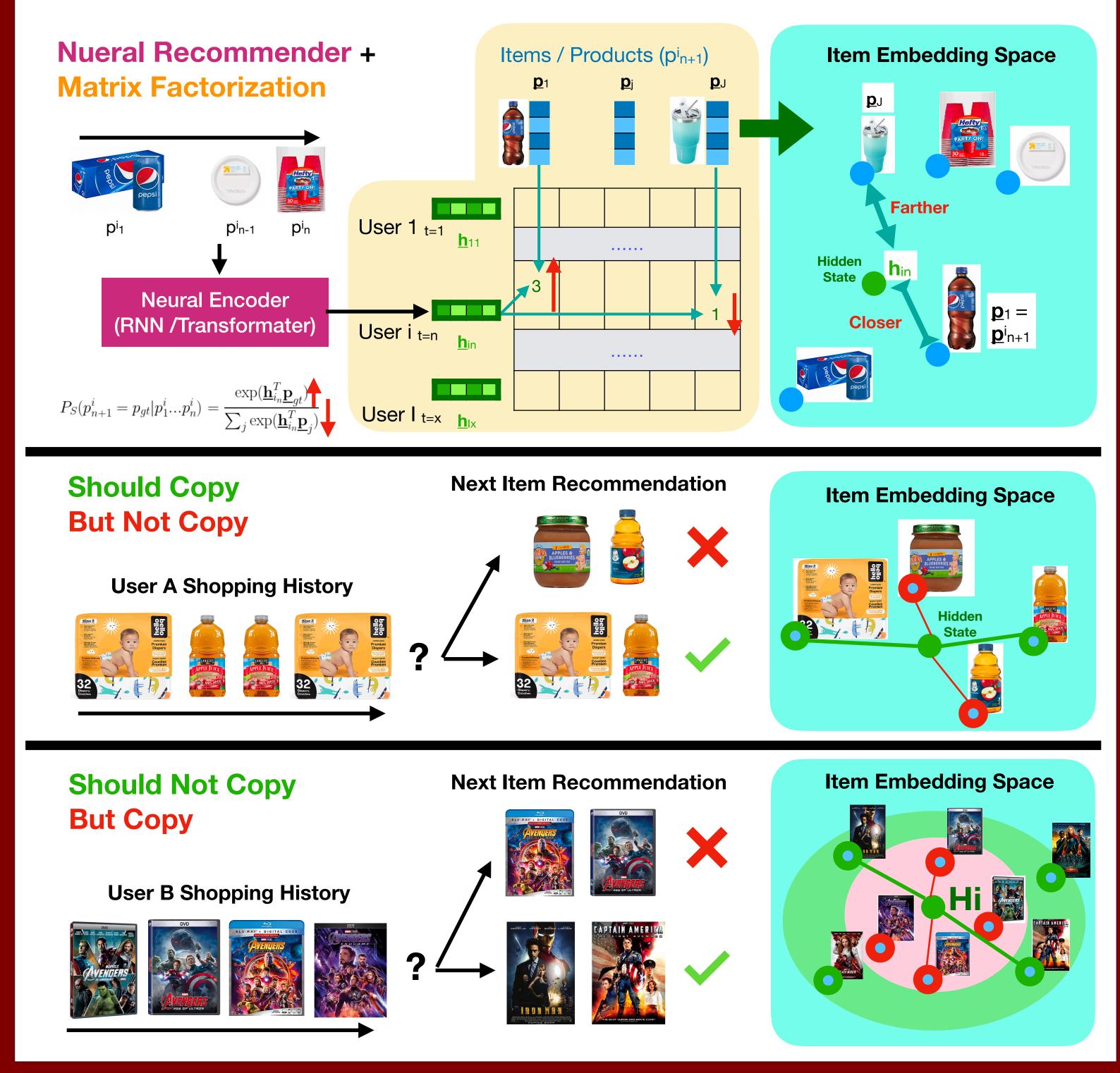


Introduction

- Did you ever experience this:
 - Training on a dataset with lots of repeated items, your STOA recommenders cannot learn to copy the items properly ?
 - Training on a dataset without repeated items, your STOA recommenders still keeps copying items ?????
- In this work, we find that the problem comes from the universally-used output softmax layer !!!!!!

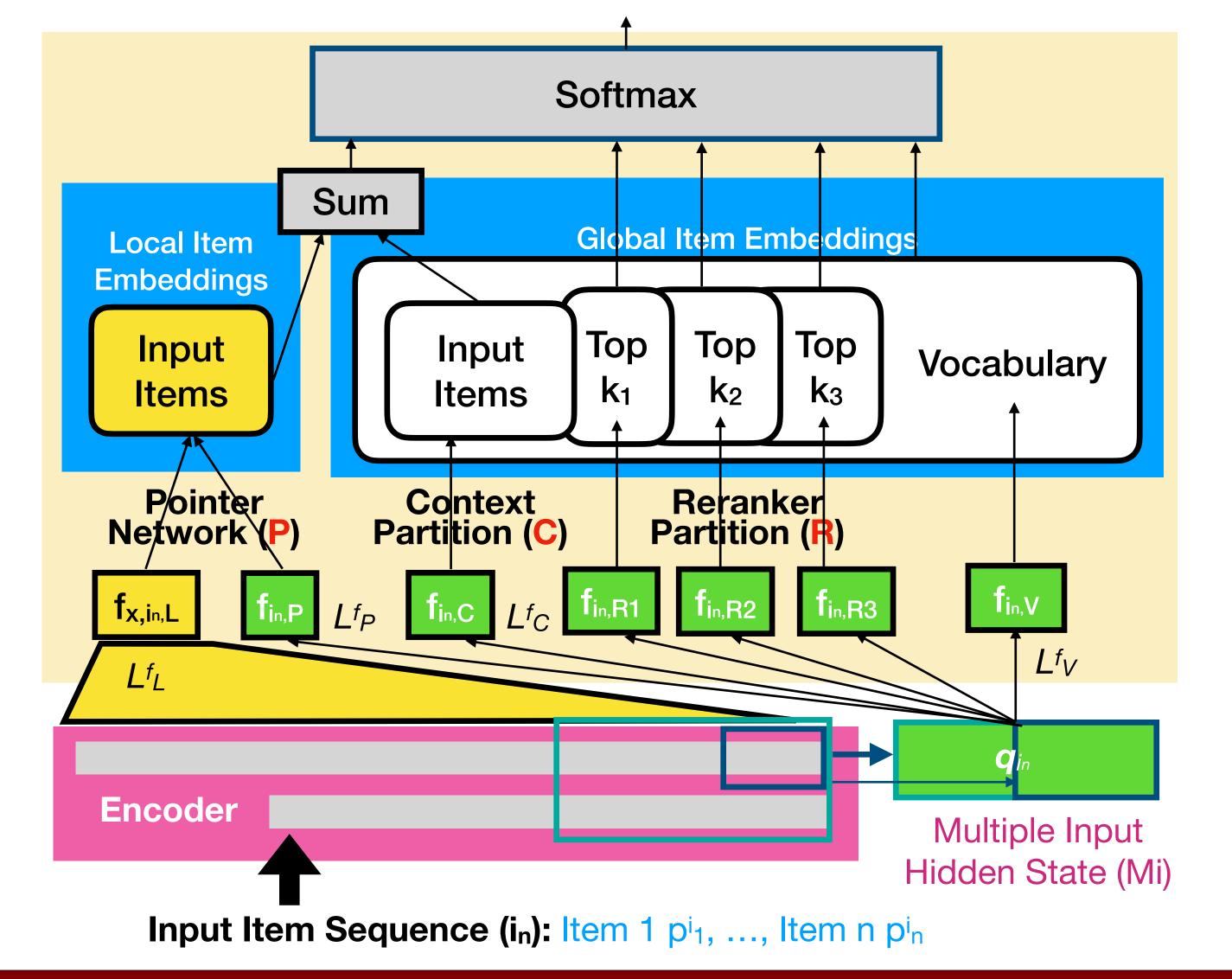


Softmax Bottleneck Problems



Solutions

- 1. Softmax (Original SASRec or GRU4Rec)
- 2. RepeatNet [2] (i.e., Pointer Network)
- 3. MoS (Mixture of Softmax) [3]
- 4. Softmax w/o Duplication [4]
- 5. Softmax + **C** (Context Partition)
- 6. Softmax + CP (Pointer Network)
- 7. Softmax + CPR (Reranker Partition)
- 8. Softmax + CPR:k₁,k₂,k₃ + Mi (Multiple Input Hidden State) [1]



Experiments

		Amazon-2014					MovieLens				Twitch-100k		Valm 2019		
		Beauty		Books		Video Games		10m		1m		I WITCH-IOOK		Yelp-2018	
		NDCG	HR	NDCG	HR	NDCG	HR	NDCG	HR	NDCG	HR	NDCG	HR	NDCG	HR
	Softmax	1.16	2.19	3.30	5.81	4.12	7.97	15.72	26.67	16.75	29.45	8.41	15.51	1.66	3.36
SASRec	Softmax + Mi	1.18	2.20	3.23	5.77	3.79	7.48	15.80	26.69	16.67	29.06	8.08	15.03	1.67	3.36
	Softmax + C	1.41	2.41	3.83	6.46	4.41	8.27	19.12	31.13	20.70	34.19	9.14	16.39	1.94	3.82
	Softmax + CP	1.45	2.52	3.94	6.71	4.54	8.59	18.62	30.51	20.69	34.67	9.45	16.93	2.04	3.91
	Softmax + CPR:100	1.38	2.42	4.15	6.89	4.57	8.69	19.32	31.32	20.79	34.25	9.11	15.94	2.22	4.24
	Softmax + CPR:100 + Mi	1.37	2.41	4.30	7.20	4.47	8.40	18.90	30.73	20.82	34.49	9.06	15.91	2.21	4.24
	Softmax + CPR:20,100,500 + Mi	1.39	2.43	3.93	6.60	4.46	8.58	19.19	30.93	20.48	33.61	8.58	14.88	2.20	4.27
	Mixture of Softmax (MoS)	1.19	2.24	3.24	5.75	3.74	7.35	15.88	26.82	17.05	29.83	8.17	15.19	1.69	3.42
	Softmax w/o Duplication [22]	1.34	2.42	3.73	6.27	4.42	8.35	18.35	30.19	20.06	33.81	9.01	16.13	1.85	3.64
GRU4Rec	Softmax	1.43	2.67	3.09	5.70	4.45	8.64	14.19	24.17	16.05	28.03	8.36	15.55	1.68	3.42
	Softmax + Mi	1.47	2.69	3.30	5.92	4.58	8.79	14.58	25.04	16.55	28.94	8.03	14.98	1.76	3.52
	Softmax + C	1.59	2.88	3.97	6.66	4.95	9.36	17.78	29.24	20.01	32.86	9.25	16.50	2.02	3.92
	Softmax + CP	1.61	2.94	4.07	6.83	5.10	9.41	17.46	28.64	19.63	32.91	9.14	16.09	2.00	3.85
	Softmax + CPR:100	1.78	3.22	4.28	7.06	5.05	9.49	17.78	29.01	20.35	33.73	9.04	15.82	2.27	4.35
	Softmax + CPR:100 + Mi	1.72	3.15	4.42	7.23	5.07	9.43	18.09	29.43	21.00	34.52	9.32	16.20	2.37	4.5
	Softmax + CPR:20,100,500 + Mi	1.73	3.11	4.37	7.14	5.02	9.33	17.87	29.09	20.44	33.63	8.80	15.20	2.31	4.39
	Mixture of Softmax (MoS)	1.46	2.73	3.15	5.76	4.06	8.00	14.40	24.50	16.14	28.06	7.90	14.69	1.73	3.50
	Softmax w/o Duplication [22]	1.60	2.91	3.71	6.26	4.83	9.09	16.85	27.68	18.54	31.72	8.94	16.03	1.94	3.80
RepeatNet	-	1.75	2.88	3.94	6.36	4.47	8.36	18.09	29.20	18.71	31.08	8.52	14.91	2.02	3.88

Table 2: We compare the test performance (%) of NDCG@10 and HR@10 in 7 datasets without duplicated items. C, P, R means context partition, pointer network, and reranker partition, respectively. 20,100,500 refers to $k_1 = 20$, $k_2 = 100$ and $k_3 = 500$; Mi means the multiple input hidden state enhancement. The best values given the same neural encoder are highlighted.

Softmax 85.66 90.42 29.28 40.39 15.67 20.28 22.44 26.60 35.7 Softmax + Mi 85.68 89.72 29.72 40.72 15.77 20.47 22.64 26.80 36.66 Softmax + C 86.25 91.15 32.23 45.15 16.32 21.13 25.29 30.36 37.21 Softmax + CP 85.60 89.75 32.88 45.68 16.30 21.05 25.58 30.50 37.41 Softmax + CPR:100 87.40 91.09 33.03 46.17 16.43 21.31 25.73 30.70 37.70 Softmax + CPR:100 + Mi 88.19 92.19 33.41 46.29 16.48 21.39 25.74 30.58 39.00 Softmax + CPR:20,100,500 + Mi 88.81 92.07 33.92 46.64 16.34 21.15 25.58 30.22 39.2 Softmax w/o Duplication [22] 80.13 82.89 3.92 7.00 4.89 9.15 4.29 6.28<			Bridge to Algebra		Gowalla		Steam		Tmall-buy		Yoochoose-clicks	
Softmax + Mi85.6889.7229.7240.7215.7720.4722.6426.8036.63Softmax + C86.2591.1532.2345.1516.3221.1325.2930.3637.24Softmax + CP85.6089.7532.8845.6816.3021.0525.5830.5037.44SASRecSoftmax + CPR:10087.4091.0933.0346.1716.4321.3125.7330.7037.74Softmax + CPR:100 + Mi88.1992.1933.4146.2916.4821.3925.7430.5839.00Softmax + CPR:20,100,500 + Mi88.8192.0733.9246.6416.3421.1525.5830.2239.2Mixture of Softmax (MoS)84.7789.7829.7440.8715.9020.4923.0727.2835.55Softmax w/o Duplication [22]80.1382.893.927.004.899.154.296.2817.00Softmax + CPSoftmax + CP85.6689.7532.2345.1816.2921.0425.1830.2537.4Softmax + CP85.6692.3533.0146.0816.3621.1525.7730.3438.33Softmax + CPR:10088.5692.3533.0146.0816.3621.1525.7730.3438.33Softmax + CPR:100 + Mi88.8192.1933.2246.0916.4921.3525.5430.0138.7Softmax + CPR:100 + Mi88.8192.19 <t< td=""><td></td><td></td><td>NDCG</td><td>HR</td><td>NDCG</td><td>HR</td><td>NDCG</td><td>HR</td><td>NDCG</td><td>HR</td><td>NDCG</td><td>HR</td></t<>			NDCG	HR	NDCG	HR	NDCG	HR	NDCG	HR	NDCG	HR
Softmax + C 86.25 91.15 32.23 45.15 16.32 21.13 25.29 30.36 37.20 SASRec Softmax + CP 85.60 89.75 32.88 45.68 16.30 21.05 25.58 30.50 37.40 SASRec Softmax + CPR:100 87.40 91.09 33.03 46.17 16.43 21.31 25.73 30.70 37.47 Softmax + CPR:100 + Mi 88.19 92.19 33.41 46.29 16.48 21.39 25.74 30.58 39.03 Softmax + CPR:20,100,500 + Mi 88.81 92.07 33.92 46.64 16.34 21.15 25.88 30.22 39.2 Mixture of Softmax (MoS) 84.77 89.78 29.74 40.87 15.90 20.49 23.07 27.28 35.55 Softmax w/o Duplication [22] 80.13 82.89 3.92 7.00 4.89 9.15 4.29 6.24 36.14 Softmax + Mi 84.68 89.01 27.99 39.06 15.69 20.26 21.76 26.05 36.33 Softmax + CP 85.		Softmax	85.66	90.42	29.28	40.39	15.67	20.28	22.44	26.60	35.74	57.28
Softmax + CP 85.60 89.75 32.88 45.68 16.30 21.05 25.58 30.50 37.42 SASRec Softmax + CPR:100 87.40 91.09 33.03 46.17 16.43 21.31 25.73 30.70 37.72 Softmax + CPR:100 + Mi 88.19 92.19 33.41 46.29 16.48 21.39 25.74 30.58 39.02 Softmax + CPR:20,100,500 + Mi 88.81 92.07 33.92 46.64 16.34 21.15 25.58 30.22 39.2 Mixture of Softmax (MoS) 84.77 89.78 29.74 40.87 15.90 20.49 23.07 27.28 35.55 Softmax w/o Duplication [22] 80.13 82.89 3.92 7.00 4.89 9.15 4.29 6.28 17.00 Softmax + Mi 84.68 89.01 27.99 39.06 15.69 20.26 21.76 26.05 36.33 Softmax + CP 85.86 89.75 32.23 45.18 16.22 21.04 25.18 30.25 37.44 Softmax + CP 85.86 92.		Softmax + Mi	85.68	89.72	29.72	40.72	15.77	20.47	22.64	26.80	36.62	57.93
SASRec Softmax + CPR:100 87.40 91.09 33.03 46.17 16.43 21.31 25.73 30.70 37.77 Softmax + CPR:100 + Mi 88.19 92.19 33.41 46.29 16.48 21.39 25.74 30.58 39.00 Softmax + CPR:20,100,500 + Mi 88.81 92.07 33.92 46.64 16.34 21.15 25.58 30.22 39.2 Mixture of Softmax (MoS) 84.77 89.78 29.74 40.87 15.90 20.49 23.07 27.28 35.55 Softmax w/o Duplication [22] 80.13 82.89 3.92 7.00 4.89 9.15 4.29 6.28 17.00 Softmax Mix 85.10 89.23 28.37 39.48 15.35 19.88 22.06 26.42 36.14 Softmax + Mi 84.68 89.01 27.99 39.06 15.69 20.26 21.76 26.05 36.33 Softmax + CP 86.24 91.06 32.48 45.43 16.32 21.04 25.18 30.25 37.44 Softmax + CPR:100 88.56		Softmax + C	86.25	91.15	32.23	45.15	16.32	21.13	25.29	30.36	37.26	58.93
Softmax + CPR:100 + Mi 88.19 92.19 33.41 46.29 16.48 21.39 25.74 30.58 39.02 Softmax + CPR:20,100,500 + Mi 88.81 92.07 33.92 46.64 16.34 21.15 25.58 30.22 39.2 Mixture of Softmax (MoS) 84.77 89.78 29.74 40.87 15.90 20.49 23.07 27.28 35.55 Softmax w/o Duplication [22] 80.13 82.89 3.92 7.00 4.89 9.15 4.29 6.28 17.00 Softmax Mixture of Softmax 85.10 89.23 28.37 39.48 15.35 19.88 22.06 26.42 36.14 Softmax + Mi 84.68 89.01 27.99 39.06 15.69 20.26 21.76 26.05 36.33 Softmax + CP 86.24 91.06 32.48 45.43 16.32 21.04 25.18 30.25 37.44 Softmax + CPR:100 88.56 92.35 33.01 46.08 16.36 21.15 25.77 30.34 38.35 Softmax + CPR:100 + Mi 88.81 </td <td></td> <td>Softmax + CP</td> <td>85.60</td> <td>89.75</td> <td>32.88</td> <td>45.68</td> <td>16.30</td> <td>21.05</td> <td>25.58</td> <td>30.50</td> <td>37.43</td> <td>59.02</td>		Softmax + CP	85.60	89.75	32.88	45.68	16.30	21.05	25.58	30.50	37.43	59.02
Softmax + CPR:20,100,500 + Mi 88.81 92.07 33.92 46.64 16.34 21.15 25.58 30.22 39.2 Mixture of Softmax (MoS) 84.77 89.78 29.74 40.87 15.90 20.49 23.07 27.28 35.57 Softmax w/o Duplication [22] 80.13 82.89 3.92 7.00 4.89 9.15 4.29 6.28 17.00 Softmax Mixture of Softmax 85.10 89.23 28.37 39.48 15.35 19.88 22.06 26.42 36.17 Softmax + Mi 84.68 89.01 27.99 39.06 15.69 20.26 21.76 26.05 36.37 Softmax + C 85.86 89.75 32.23 45.18 16.29 21.04 25.18 30.25 37.4 GRU4Rec Softmax + CPR:100 88.56 92.35 33.01 46.08 16.36 21.15 25.77 30.34 38.37 Softmax + CPR:100 + Mi 88.81 92.19 33.22 46.09 16.49 21.35 25.54 30.01 38.7 30.43 38.55	SASRec	Softmax + CPR:100	87.40	91.09	33.03	46.17	16.43	21.31	25.73	30.70	37.79	59.15
Mixture of Softmax (MoS) 84.77 89.78 29.74 40.87 15.90 20.49 23.07 27.28 35.57 Softmax w/o Duplication [22] 80.13 82.89 3.92 7.00 4.89 9.15 4.29 6.28 17.00 Softmax Softmax 85.10 89.23 28.37 39.48 15.35 19.88 22.06 26.42 36.14 Softmax + Mi 84.68 89.01 27.99 39.06 15.69 20.26 21.76 26.05 36.34 Softmax + C 85.86 89.75 32.23 45.18 16.29 21.04 25.18 30.25 37.44 Softmax + CP 86.24 91.06 32.48 45.43 16.32 21.06 25.45 30.36 37.94 GRU4Rec Softmax + CPR:100 88.56 92.35 33.01 46.08 16.36 21.15 25.77 30.34 38.33 Softmax + CPR:100 + Mi 88.81 92.19 33.22 46.09 16.49 21.35 25.54 30.01 38.7 Softmax + CPR:20,100,500 + Mi 89.46<		Softmax + CPR:100 + Mi	88.19	92.19	33.41	46.29	16.48	21.39	25.74	30.58	39.03	59.69
Softmax w/o Duplication [22] 80.13 82.89 3.92 7.00 4.89 9.15 4.29 6.28 17.00 Softmax 85.10 89.23 28.37 39.48 15.35 19.88 22.06 26.42 36.14 Softmax + Mi 84.68 89.01 27.99 39.06 15.69 20.26 21.76 26.05 36.34 Softmax + C 85.86 89.75 32.23 45.18 16.29 21.04 25.18 30.25 37.44 Softmax + CP 86.24 91.06 32.48 45.43 16.32 21.06 25.45 30.36 37.94 GRU4Rec Softmax + CPR:100 88.56 92.35 33.01 46.08 16.36 21.15 25.77 30.34 38.33 Softmax + CPR:100 + Mi 88.81 92.19 33.22 46.09 16.49 21.35 25.54 30.01 38.7 Softmax + CPR:20,100,500 + Mi 89.46 92.29 33.18 45.93 16.41 21.19 25.		Softmax + CPR:20,100,500 + Mi	88.81	92.07	33.92	46.64	16.34	21.15	25.58	30.22	39.26	59.68
Softmax 85.10 89.23 28.37 39.48 15.35 19.88 22.06 26.42 36.14 Softmax + Mi 84.68 89.01 27.99 39.06 15.69 20.26 21.76 26.05 36.34 Softmax + C 85.86 89.75 32.23 45.18 16.29 21.04 25.18 30.25 37.44 Softmax + CP 86.24 91.06 32.48 45.43 16.32 21.06 25.45 30.36 37.94 GRU4Rec Softmax + CPR:100 88.56 92.35 33.01 46.08 16.36 21.15 25.77 30.34 38.33 Softmax + CPR:100 + Mi 88.81 92.19 33.22 46.09 16.49 21.35 25.54 30.01 38.7 Softmax + CPR:20,100,500 + Mi 89.46 92.29 33.18 45.93 16.41 21.19 25.72 30.43 38.55 Mixture of Softmax (MoS) 86.11 90.30 27.91 38.60 15.89 20.41 21.50 25.75 36.34 Softmax w/o Duplication [22] 79.06 81		Mixture of Softmax (MoS)	84.77	89.78	29.74	40.87	15.90	20.49	23.07	27.28	35.59	57.07
Softmax + Mi84.6889.0127.9939.0615.6920.2621.7626.0536.34Softmax + C85.8689.7532.2345.1816.2921.0425.1830.2537.44Softmax + CP86.2491.0632.4845.4316.3221.0625.4530.3637.94GRU4RecSoftmax + CPR:10088.5692.3533.0146.0816.3621.1525.7730.3438.33Softmax + CPR:100 + Mi88.8192.1933.2246.0916.4921.3525.5430.0138.7Softmax + CPR:20,100,500 + Mi89.4692.2933.1845.9316.4121.1925.7230.4338.54Mixture of Softmax (MoS)86.1190.3027.9138.6015.8920.4121.5025.7536.34Softmax w/o Duplication [22]79.0681.673.937.054.658.724.246.3216.84		Softmax w/o Duplication [22]	80.13	82.89	3.92	7.00	4.89	9.15	4.29	6.28	17.00	27.84
Softmax + C85.8689.7532.2345.1816.2921.0425.1830.2537.44Softmax + CP86.2491.0632.4845.4316.3221.0625.4530.3637.94GRU4RecSoftmax + CPR:10088.5692.3533.0146.0816.3621.1525.7730.3438.34Softmax + CPR:100 + Mi88.8192.1933.2246.0916.4921.3525.5430.0138.7Softmax + CPR:20,100,500 + Mi89.4692.2933.1845.9316.4121.1925.7230.4338.54Mixture of Softmax (MoS)86.1190.3027.9138.6015.8920.4121.5025.7536.34Softmax w/o Duplication [22]79.0681.673.937.054.658.724.246.3216.80		Softmax	85.10	89.23	28.37	39.48	15.35	19.88	22.06	26.42	36.19	56.97
Softmax + CP 86.24 91.06 32.48 45.43 16.32 21.06 25.45 30.36 37.96 GRU4Rec Softmax + CPR:100 88.56 92.35 33.01 46.08 16.36 21.15 25.77 30.34 38.35 Softmax + CPR:100 + Mi 88.81 92.19 33.22 46.09 16.49 21.35 25.54 30.01 38.7 Softmax + CPR:20,100,500 + Mi 89.46 92.29 33.18 45.93 16.41 21.19 25.72 30.43 38.54 Mixture of Softmax (MoS) 86.11 90.30 27.91 38.60 15.89 20.41 21.50 25.75 36.34 Softmax w/o Duplication [22] 79.06 81.67 3.93 7.05 4.65 8.72 4.24 6.32 16.89		Softmax + Mi	84.68	89.01	27.99	39.06	15.69	20.26	21.76	26.05	36.39	57.15
GRU4Rec Softmax + CPR:100 88.56 92.35 33.01 46.08 16.36 21.15 25.77 30.34 38.33 Softmax + CPR:100 + Mi 88.81 92.19 33.22 46.09 16.49 21.35 25.54 30.01 38.7 Softmax + CPR:20,100,500 + Mi 89.46 92.29 33.18 45.93 16.41 21.19 25.72 30.43 38.54 Mixture of Softmax (MoS) 86.11 90.30 27.91 38.60 15.89 20.41 21.50 25.75 36.34 Softmax w/o Duplication [22] 79.06 81.67 3.93 7.05 4.65 8.72 4.24 6.32 16.84		Softmax + C	85.86	89.75	32.23	45.18	16.29	21.04	25.18	30.25	37.46	58.54
Softmax + CPR:100 + Mi88.8192.1933.2246.0916.4921.3525.5430.0138.7Softmax + CPR:20,100,500 + Mi89.4692.2933.1845.9316.4121.1925.7230.4338.54Mixture of Softmax (MoS)86.1190.3027.9138.6015.8920.4121.5025.7536.39Softmax w/o Duplication [22]79.0681.673.937.054.658.724.246.3216.89		Softmax + CP	86.24	91.06	32.48	45.43	16.32	21.06	25.45	30.36	37.90	58.76
Softmax + CPR:20,100,500 + Mi89.4692.2933.1845.9316.4121.1925.7230.4338.54Mixture of Softmax (MoS)86.1190.3027.9138.6015.8920.4121.5025.7536.34Softmax w/o Duplication [22]79.0681.673.937.054.658.724.246.3216.84	GRU4Rec	Softmax + CPR:100	88.56	92.35	33.01	46.08	16.36	21.15	25.77	30.34	38.35	59.15
Mixture of Softmax (MoS)86.1190.3027.9138.6015.8920.4121.5025.7536.39Softmax w/o Duplication [22]79.0681.673.937.054.658.724.246.3216.89		Softmax + CPR:100 + Mi	88.81	92.19	33.22	46.09	16.49	21.35	25.54	30.01	38.72	59.4 2
Softmax w/o Duplication [22] 79.06 81.67 3.93 7.05 4.65 8.72 4.24 6.32 16.80		Softmax + CPR:20,100,500 + Mi	89.46	92.29	33.18	45.93	16.41	21.19	25.72	30.43	38.54	59.20
		Mixture of Softmax (MoS)	86.11	90.30	27.91	38.60	15.89	20.41	21.50	25.75	36.39	56.97
RepeatNet - 77.44 81.70 33.83 45.88 16.28 20.90 25.67 30.17 38.00		Softmax w/o Duplication [22]	79.06	81.67	3.93	7.05	4.65	8.72	4.24	6.32	16.80	27.44
•	RepeatNet	-	77.44	81.70	33.83	45.88	16.28	20.90	25.67	30.17	38.00	58.53

Table 3: The test performance (%) in 5 datasets with duplicated items. The notations are the same as Table 2.

- 1. The improvements of Softmax + CPR + Mi are consistent across 12 large datasets and hyperparameters
 - A. 10% (4%-17%) in 5 datasets with duplicated items
 - B. 24% (8%-39%) in 7 datasets without duplicated items
- 2. The best method increases the model size very slightly.
- 3. Softmax + C \approx RepeatNet [2] \approx Softmax w/o duplication [4]

Conclusions



2. Selection of the softmax layer is much more important than selection of the encoder on average in our experiments.

3. RepeatNet / pointer network improves the performance due to the softmax bottleneck instead of the attention mechanism.

Applications

- 1. Try Softmax-CPR in RecBole to achieve new STOA
- 2. Softmax-CPR also reduces hallucination in LLM
- 3. Future work: other matrix factorization models?





[1] Haw-Shiuan Chang*, Zonghai Yao*, Alolika Gon, Hong Yu, and Andrew McCallum. 2023. "Revisiting the Architectures like Pointer Networks to Efficiently Improve the Next Word Distribution, Summarization Factuality, and Beyond". In Findings of ACL 2023

[2] Pengjie Ren, Zhumin Chen, Jing Li, Zhaochun Ren, Jun Ma, and Maarten De Rijke. 2019. Repeatnet: A repeat aware neural recommendation machine for sessionbased recommendation. In AAAI 2019

[3] Zhilin Yang, Zihang Dai, Ruslan Salakhutdinov, and William W. Cohen. 2018. Breaking the Softmax Bottleneck: A High-Rank RNN Language Model. In ICLR 2018

[4] Ming Li, Ali Vardasbi, Andrew Yates, and Maarten de Rijke. 2023. "Repetition and Exploration in Sequential Recommendation". In SIGIR 2023 https://commons.wikimedia.org/wiki/File:Stop_hand-octogon-red.svg